# A novel experiment for the quantitative measurement of $\operatorname{CSA}\left({ }^{1} \mathbf{H}_{\mathrm{N}}\right) / \mathrm{CSA}\left({ }^{15} \mathrm{~N}\right)$ cross-correlated relaxation in ${ }^{15} \mathrm{~N}$-labeled proteins* 

Marco Tessari** \& Geerten W. Vuister<br>Nijmegen SON Research Center, Department of Biophysical Chemistry, University of Nijmegen, Toernooiveld 1, 6525 ED Nijmegen, The Netherlands

Received 27 October 1999; Accepted 6 December 1999

Key words: cross-correlation, CSA, EH2, Eps15, relaxation


#### Abstract

An experiment is presented which allows for the quantitative measurement of the relaxation interference between the ${ }^{1} \mathrm{H}_{\mathrm{N}}$ CSA and ${ }^{15} \mathrm{~N}$ CSA interactions in ${ }^{15} \mathrm{~N}$ labeled proteins. A constant-time buildup scheme is used to measure the differential relaxation rate, $\eta$, between double-quantum ( DQ ) and zero-quantum ( ZQ ) ${ }^{1} \mathrm{H}_{\mathrm{N}^{-}}{ }^{15} \mathrm{~N}$ coherences. The CSA/CSA experiment was recorded at three different $\mathrm{B}_{0}$ field strengths. The $\operatorname{CSA}\left({ }^{1} \mathrm{H}_{\mathrm{N}}\right) / \mathrm{CSA}\left({ }^{15} \mathrm{~N}\right)$ crosscorrelation rate was obtained from the linear fit of the measured rate, $\eta$, versus $B_{o}^{2}$ for 77 residues of the EH2 domain from mouse Eps 15 .


The measurement of cross-correlated relaxation rates has recently attracted a great deal of interest because of the high content of structural and dynamical information related to these rates (Reif et al., 1997; Kroenke et al., 1998). For instance, the $\mathrm{H}_{\mathrm{N}}$ chemical shift anisotropy (CSA) derived from the measurement of CSA/dipolar (CSA/DD) relaxation interference in ${ }^{15} \mathrm{~N}$ labeled proteins has proved to be a very good indicator for hydrogen bonding (Tessari et al., 1997a; Tjandra and Bax, 1997). Recent solid-state NMR data on crystalline hydrates have also shown that the orientation and asymmetry of the ${ }^{1} \mathrm{H}$ CSA tensor are highly correlated with hydrogen bonding geometry (Wu et al., 1998). For biomolecules, such information would also be of major importance because of the crucial role of the hydrogen bond in molecular structure and recognition.

Here, we present a novel experiment which allows for the quantitative measurement of the relaxation interference between the ${ }^{1} \mathrm{H}_{\mathrm{N}}$ CSA and ${ }^{15} \mathrm{~N}$ CSA interactions in ${ }^{15} \mathrm{~N}$ labeled proteins. The combination of this experiment and previously reported

[^0]$\operatorname{CSA}\left({ }^{1} \mathrm{H}_{\mathrm{N}}\right) / \mathrm{DD}\left({ }^{1} \mathrm{H}_{\mathrm{N}^{-}}{ }^{15} \mathrm{~N}\right)$ and $\operatorname{CSA}\left({ }^{15} \mathrm{~N}\right) / \mathrm{DD}\left({ }^{1} \mathrm{H}_{\mathrm{N}}-\right.$ ${ }^{15} \mathrm{~N}$ ) experiments (Tjandra et al., 1996; Tessari et al., 1997a,b; Tjandra and Bax, 1997) will provide a more complete picture of the ${ }^{1} \mathrm{H}_{\mathrm{N}}$ CSA tensor.

The experiment is based on the measurement of the difference between the relaxation rates of doublequantum ( $\Gamma^{\mathrm{DQ}}$ ) and zero-quantum ( $\Gamma^{\mathrm{ZQ}}$ ) ${ }^{1} \mathrm{H}_{\mathrm{N}}{ }^{-15} \mathrm{~N}$ coherences. For a multi-spin system the differential rate, $\eta$, can be written as (Konrat and Sterk, 1993; Kumar and Kumar, 1996; Norwood et al., 1999):

$$
\begin{equation*}
\eta=\frac{\Gamma^{D Q}-\Gamma^{Z Q}}{2}=\eta^{c c}+\sigma^{d d}+\eta^{d d}+\eta^{\text {exch }} \tag{1}
\end{equation*}
$$

where $\eta^{c c}$, $\sigma^{d d}$, and $\eta^{d d}$ indicate the $\operatorname{CSA}\left({ }^{1} \mathrm{H}_{\mathrm{N}}\right) /$ CSA $\left({ }^{15} \mathrm{~N}\right)$ cross-correlation rate, the ${ }^{1} \mathrm{H}_{\mathrm{N}}{ }^{15} \mathrm{~N}$ crossrelaxation rate, and the sum of the cross-correlation rates between dipolar interactions involving other spins, $i$, close to the ${ }^{1} \mathrm{H}_{\mathrm{N}^{-}}{ }^{15} \mathrm{~N}$ pair, respectively. The last term, $\eta^{\text {exch }}$, represents the cross-correlation rate between two rank-1 relaxation mechanisms, namely ${ }^{15} \mathrm{~N}$ and ${ }^{1} \mathrm{H}$ chemical exchange. These rates are given by the following expressions:

$$
\begin{equation*}
\eta^{c c}=\frac{8}{45} \gamma_{H} \gamma_{N} \Delta \sigma_{N} \Delta \sigma_{H} B_{o}^{2} J_{H N}(0) \tag{2a}
\end{equation*}
$$



Figure 1. Pulse scheme for the quantitative measurement of relaxation interference effects between ${ }^{1} \mathrm{H}_{\mathrm{N}} \mathrm{CSA}$ and ${ }^{15} \mathrm{~N}$ CSA. Narrow and wide pulses correspond to flip angles of $90^{\circ}$ and $180^{\circ}$, respectively. Scheme A is used to record the magnetization terms arising from $\operatorname{CSA}\left({ }^{1} \mathrm{H}_{\mathrm{N}}\right) / \mathrm{CSA}\left({ }^{15} \mathrm{~N}\right)$ cross correlation in the period $\Delta$, while scheme B is used for the reference experiment. The phase of all pulses is assumed $x$, unless indicated. Phase cycling: $\phi_{1}=y,-y ; \phi_{2}=8(x), 8(y), 8(-x), 8(-y) ; \phi_{3}=4(x), 4(-x)$ (scheme A) or $\phi_{3}=4(y), 4(-y)$ (scheme B); $\phi_{4}=2(x), 2(-x)$ (scheme A) or $\phi_{4}=2(y), 2(-y)$ (scheme B); $\phi_{5}=x ; \phi_{6}=16(x), 16(-x) ; \phi_{7}=32(x), 32(y), 32(-x), 32(-y)$; receiver $=R, \underline{R}, R, \underline{R}, \underline{R}, \underline{R}, \underline{R}, R$, where $R=x,-x,-x, x$ and $\underline{R}=-x, x, x,-x$. Quadrature detection in the $t_{1}$ dimension is accomplished by incrementing $\phi_{5}$ in the States-TPPI manner. Delay durations: $\mathrm{T}=30 \mathrm{~ms} ; \delta=2.75 \mathrm{~ms} ; \Delta=20,30 \mathrm{~ms}$ at $11.7 \mathrm{~T} ; 12.8,25.6 \mathrm{~ms}$ at 14.1 T ; $15,25 \mathrm{~ms}$ at 17.6 T . All gradients are sine-bell shaped; $\mathrm{G}_{1,2,3,4}=1.0 \mathrm{~ms}, 20 \mathrm{G} / \mathrm{cm} ; 1.0 \mathrm{~ms}, 17 \mathrm{G} / \mathrm{cm} ; 1.5 \mathrm{~ms}, 27 \mathrm{G} / \mathrm{cm} ; 1.0 \mathrm{~ms},-7 \mathrm{G} / \mathrm{cm}$. A REBURP pulse (Geen and Freeman, 1991) with the center of its excitation profile at 8.1 ppm and a width of 4.76 ms at 500 MHz is used to selectively refocus the signals in the amide region. In the reverse INEPT step a 3-9-19-19-9-3 WATERGATE refocusing pulse is used (Sklenar et al., 1993). Typically 256 scans were recorded for each hypercomplex increment, yielding a total experimental time of $\sim 20 \mathrm{~h}$.

$$
\begin{align*}
\sigma^{d d}= & \frac{1}{10}\left(\frac{\mu_{o}}{4 \pi}\right)^{2}\left(\frac{\gamma_{H} \gamma_{N} \hbar}{r_{H N}^{3}}\right)^{2}\left[6 J_{H N H N}\right. \\
& \left.\times\left(\omega_{H}+\omega_{N}\right)-J_{H N H N}\left(\omega_{H}-\omega_{N}\right)\right]  \tag{2b}\\
\eta^{d d}= & \frac{2}{5}\left(\frac{\mu_{o}}{4 \pi}\right)^{2} \gamma_{H} \gamma_{N} \hbar^{2} \sum_{i} \frac{\gamma_{i}^{2}}{r_{N i}^{3} r_{H i}^{3}}\left[J_{H i N i}(0)\right. \\
& \left.+\frac{3}{4} J_{H i N i}\left(\omega_{i}\right)\right]  \tag{2c}\\
\eta^{\text {exch }}= & 2 p_{A} p_{B} \delta \omega_{N} \delta \omega_{H} \tau_{\text {exch }} \\
= & 2 p_{A} p_{B} \gamma_{N} \gamma_{H} \delta \sigma_{N}^{i s o} \delta \sigma_{H}^{i s o} B_{o}^{2} \tau_{\text {exch }} \tag{2d}
\end{align*}
$$

where $\Delta \sigma_{H}$ and $\Delta \sigma_{N}$ indicate the anisotropy of the chemical shift $\left(\sigma_{\|}-\sigma_{\perp}\right)$ for the ${ }^{1} \mathrm{H}_{\mathrm{N}}$ and ${ }^{15} \mathrm{~N}$ nuclei, respectively. The symbols $B_{o}, \gamma_{H}, \gamma_{N}, \gamma_{i}, r_{H N}, r_{H i}$, and $r_{N i}$ have their usual meanings, where $i$ is defined as above. $J_{H N}(\omega), J_{H i N i}(\omega)$ and $J_{H N H N}(\omega)$ denote the spectral density for the CSA-CSA cross-correlation, the dipolar cross-correlation, and the dipolar autocorrelation, respectively. Expression 2d holds in the case of fast conformational exchange between two sites with populations $p_{A}$ and $p_{B}$ and an exchange correlation time $\tau_{\text {exch. }}$. The symbols $\delta \sigma_{N}^{i s o}$ and $\delta \sigma_{H}^{i s o}$ denote the difference in ${ }^{15} \mathrm{~N}$ and ${ }^{1} \mathrm{H}$ isotropic chemical shift, respectively.

In the simple case of isotropic motion of a rigid body, the following equalities hold:

$$
\begin{align*}
J_{H N}(\omega) & =J(\omega)\left(\frac{3 \cos ^{2} \theta_{H N}-1}{2}\right) \\
& =\frac{\tau_{c}}{1+\omega^{2} \tau_{c}^{2}}\left(\frac{3 \cos ^{2} \theta_{H N}-1}{2}\right)  \tag{3a}\\
J_{H i N i}(\omega) & =J(\omega)\left(\frac{3 \cos ^{2} \theta_{H i N i}-1}{2}\right) \\
& =\frac{\tau_{c}}{1+\omega^{2} \tau_{c}^{2}}\left(\frac{3 \cos ^{2} \theta_{H i N i}-1}{2}\right)  \tag{3b}\\
J_{H N H N}(\omega) & =J(\omega)=\frac{\tau_{c}}{1+\omega^{2} \tau_{c}^{2}} \tag{3c}
\end{align*}
$$

where $\tau_{c}$ indicates the rotational correlation time and $\theta_{H N}$ and $\theta_{H i N i}$ denote the angle between the axes of the two CSA tensors, assumed here as being axially symmetric (Gerald et al., 1993), or the two dipolar interactions, respectively.

Figure 1 shows the pulse scheme used for the quantitative measurement of the $\operatorname{CSA}\left({ }^{1} \mathrm{H}_{\mathrm{N}}\right) / \mathrm{CSA}\left({ }^{15} \mathrm{~N}\right)$ relaxation interference. Rather than measuring $\Gamma^{\mathrm{DQ}}$ and $\Gamma^{\mathrm{ZQ}}$ separately, as recently proposed by Norwood et al. (1999), our experiment allows the direct observation of the terms generated by the


Figure 2. (A) Buildups of the ratio $\mathrm{I}^{c c} / \mathrm{I}^{r e f}$ for residue $\mathrm{Asn}^{157}$ at 11.7 T (circle), 14.1 T (triangle) and 17.6 T (square). The curves obtained from the linear fits of the ratio $I^{c c} / I^{r e f}$ versus the time interval $\Delta$, according to Equation 4, are shown. (B) Linear fit of the measured $\eta$ rate versus the square of the field strength, $\mathrm{B}_{o}$, for residues Phe ${ }^{145}$ (triangle), Leu ${ }^{156}$ (square) and Asn ${ }^{157}$ (circle) in mEH2.
$\operatorname{CSA}\left({ }^{1} \mathrm{H}_{\mathrm{N}}\right) / \mathrm{CSA}\left({ }^{15} \mathrm{~N}\right)$ cross-correlated relaxation. A constant-time buildup scheme is used, as previously employed for measuring the $\operatorname{CSA}\left({ }^{1} \mathrm{H}_{\mathrm{N}}\right) / \mathrm{DD}\left({ }^{1} \mathrm{H}_{\mathrm{N}^{-}}\right.$ $\left.{ }^{15} \mathrm{~N}\right)$ and $\operatorname{CSA}\left({ }^{15} \mathrm{~N}\right) / \mathrm{DD}\left({ }^{1} \mathrm{H}_{\mathrm{N}^{-}}{ }^{15} \mathrm{~N}\right)$ cross-correlation rates (Tessari et al., 1997a,b).

Between time points $a$ and $b$ of the pulse scheme, the $2 N_{x} H_{x}$ term of the density operator, corresponding to the superposition of DQ and $\mathrm{ZQ}{ }^{1} \mathrm{H}_{\mathrm{N}^{-}}{ }^{15} \mathrm{~N}$ coherences, precesses in the transverse plane for a period of duration T. During the time interval $\Delta$, as a consequence of the differential relaxation of DQ and ZQ coherences, $2 N_{x} H_{x}$ coherence is partially converted into $2 N_{y} H_{y}$ coherence. Neither scalar coupling nor chemical shift evolution contribute to the creation of the $2 N_{y} H_{y}$ term, since they are both refocused at time point $b$ of the sequence. Depending on the phases of the ${ }^{15} \mathrm{~N} 90^{\circ}$ and ${ }^{1} \mathrm{H} 90^{\circ}$ pulses following time point $b$, the $2 N_{y} H_{y}$ term (scheme A) or the $2 N_{x} H_{x}$ term (scheme B) can be selected. After the purging gradient $\mathrm{G}_{3}$, a HSQC-like sequence is employed for chemical shift labeling and acquisition.

Scheme B of the experiment is used to record the reference spectrum with $\Delta=0$. Because of the interconversion of DQ and ZQ coherences, no net differential relaxation occurs, and no $2 N_{y} H_{y}$ term is present at time point $b$ of the sequence.

The ratio of the signal intensities measured with the two schemes, $I^{c c}$ and $I^{r e f}$, is given by:

$$
\begin{align*}
\frac{I^{c c}}{I^{r e f}} & =\frac{C \exp (-\lambda T) \sinh (-\eta \Delta)}{C \exp (-\lambda T)} \\
& =\sinh (-\eta \Delta) \approx-\eta \Delta \tag{4}
\end{align*}
$$

where $\lambda$ denotes the $\mathrm{DQ} / \mathrm{ZQ}$ auto-relaxation rate, $\eta$ is defined as in Equation 1 and the proportionality factor $C$ resulting from the experimental setup is the same for both schemes since the number of pulses and the duration of delays are identical.

A buildup curve of the ratio $I^{c c} / I^{r e f}$ can be obtained by recording several experiments at different values of the delay $\Delta$ (scheme A ), and one reference spectrum (scheme B). A linear fit of the buildup curve provides the value of $\eta$. Assuming a typical value of -0.2 for the ${ }^{15} \mathrm{~N}-\left\{{ }^{1} \mathrm{H}_{\mathrm{N}}\right\}$ NOE and of 0.7 s for ${ }^{15} \mathrm{~N} \mathrm{~T}_{1}$ yields a cross relaxation rate $\sigma^{d d} \sim 0.015 \mathrm{~s}^{-1}$, well below the experimental error (vide infra). Therefore, the contribution of $\sigma^{d d}$ to the value of $\eta$ will not be considered in the following. For biomolecules, $J_{H i N i}\left(\omega_{i}\right)$ can be neglected from Equation 2c, in which case Equations 1 and 2 show that $\eta$ depends linearly on the square of the field. By measuring $\eta$ at different field strengths it is possible to separate the contribution of the field-independent term, $\eta^{d d}$, from $\eta^{c c}+\eta^{\text {exch }}$.

The CSA/CSA experiment was recorded on a 1.5 mM solution of uniformly ${ }^{15} \mathrm{~N}$ labeled EH2 from mouse Eps15 (mEH2) in acetic buffer at pH 5.1 , $100 \mathrm{mM} \mathrm{NaCl}, 95 \%{ }^{1} \mathrm{H}_{2} \mathrm{O}, 5 \%{ }^{2} \mathrm{H}_{2} \mathrm{O}, \mathrm{T}=288 \mathrm{~K}$, using Varian Inova spectrometers at 11.7 and 17.6 T and a Bruker DRX spectrometer at 14.1 T. The buildup curve of the ratio $I^{c c} / I^{r e f}$ for residue Asn ${ }^{157}$ at three field strengths is shown in Figure 2A. A change in the sign of the slope is observed increasing the field strength from 11.7 T to 17.6 T , indicating that the rates $\left(\eta^{c c}+\eta^{e x c h}\right)$ and $\eta^{d d}$ have opposite signs. Figure $2 B$ shows the fit of the rate $\eta$ as a function of $B_{o}^{2}$ for residues $\mathrm{Phe}^{145}, \mathrm{Leu}^{156}$, and $\mathrm{Asn}^{157}$. The two


Figure 3. Values of $\left(\eta^{\mathrm{cc}}+\eta^{\text {exch }}\right) / \mathrm{B}_{\mathrm{O}}^{2}(\mathrm{~A})$ and $\eta^{\mathrm{dd}}(\mathrm{B})$ as a function of residue number in mEH 2 . Residue Ala ${ }^{123}$ is indicated.
contributions $\left(\eta^{c c}+\eta^{e x c h}\right) / B_{o}^{2}$ and $\eta^{d d}$ correspond to the slope and intercept of these fits, respectively. For mEH 2 , data were obtained for 77 non-overlapping signals out of 95 non-proline residues. The values of $\left(\eta^{c c}+\eta^{\text {exch }}\right) / B_{o}^{2}$ and $\eta^{d d}$ are shown in Figure 3 as a function of the residue number. The magnitude of $\left(\eta^{c c}+\eta^{e x c h}\right) / B_{o}^{2}$ for the residues located in the structured regions of mEH 2 spans a range of $0.005-0.025 \mathrm{~s}^{-1} \mathrm{~T}^{-2}$, with an average value of $0.008 \mathrm{~s}^{-1} \mathrm{~T}^{-2}$. An extreme value of $\left(\eta^{c c}+\eta^{\text {exch }}\right) / B_{o}^{2}$ is found for residue $\mathrm{Ala}^{123}$ (cf. Figure 3), probably as a consequence of the $\eta^{\text {exch }}$ contribution. This observation is consistent with the presence of chemical exchange for this residue, as indicated by the analysis of ${ }^{15} \mathrm{~N}$ relaxation data. No significant chemical exchange was detected for the other residues, for which we can safely neglect $\eta^{\text {exch }}$. We find that the rate $\eta^{c c} / B_{o}^{2}$ is positive for most residues, which is in agreement with the single observation by Norwood et al. (1999). Using ${ }^{15} \mathrm{~N}$ CSA values obtained from ${ }^{15} \mathrm{~N}$ relaxation studies, a rotational correlation time $\tau_{c}$ of $\sim 9 \mathrm{~ns}$, and assuming $\Delta \sigma_{\mathrm{H}}$ of 10 ppm , the calculated $\eta^{c c} / B_{o}^{2}$ rates fall in the $0.007-$ $0.009 \mathrm{~s}^{-1} \mathrm{~T}^{-2}$ range. A complete analysis of the results of the $\operatorname{CSA}\left({ }^{1} \mathrm{H}_{\mathrm{N}}\right) / \mathrm{CSA}\left({ }^{15} \mathrm{~N}\right)$ experiment, in combination with the results of the $\operatorname{CSA}\left({ }^{1} \mathrm{H}_{\mathrm{N}}\right) / \mathrm{DD}\left({ }^{1} \mathrm{H}_{\mathrm{N}}{ }^{15} \mathrm{~N}\right)$ and $\mathrm{CSA}\left({ }^{15} \mathrm{~N}\right) / \mathrm{DD}\left({ }^{1} \mathrm{H}_{\mathrm{N}}{ }^{-15} \mathrm{~N}\right)$ experiments, will yield a more detailed understanding of the CSA of individual ${ }^{15} \mathrm{~N}$ and ${ }^{1} \mathrm{H}$ spins in a protein. This analysis is currently in progress, and will be reported elsewhere.

## Acknowledgements

We thank Prof. Cees Hilbers for his stimulating interest. The data at 17.6 T were recorded at the SONNMR Large Scale Facility in Utrecht.

## References

Geen, H. and Freeman, R. (1991) J. Magn. Reson., 114, 93-141.
Gerald, R., Bernhard, T., Haeberlen, U., Rendell, J. and Opella, S.J. (1993) J. Am. Chem. Soc., 115, 772-882.

Konrat, R. and Sterk, H. (1993) Chem. Phys. Lett., 203, 75-80.
Kroenke, C.D., Loria, J.P., Lee, L.K., Rance, M. and Palmer III, A.G. (1998) J. Am. Chem. Soc., 12, 7905-7915.

Kumar, P. and Kumar, A. (1996) J. Magn. Reson., A119, 29-37.
Norwood, T.J., Tillet, M.L. and Lian, L. (1999) Chem. Phys. Lett., 300, 429-434.
Reif, B., Hennig, M. and Griesinger, C. (1997) Science, 276, 12301233.

Sklenar, V., Piotto, M., Leppik, R. and Saudek, V. (1993) J. Magn. Reson., A102, 241-245.
Tessari, M., Vis, H., Boelens, R., Kaptein, R. and Vuister, G.W. (1997a) J. Am. Chem. Soc., 119, 8985-8990.
Tessari, M., Mulder F.A.A., Boelens, R. and Vuister G.W. (1997b) J. Magn. Reson., 127, 128-133.

Tjandra, N., Szabo, A. and Bax, A. (1996) J. Am. Chem. Soc., 118, 6986-6991.
Tjandra, N. and Bax, A. (1997) J. Am. Chem. Soc., 119, 8076-8082.
Wu, G., Freure, C.J. and Verdurand, E. (1998) J. Am. Chem. Soc., 120, 13187-13193.


[^0]:    *This paper is dedicated to the memory of Gino Tessari.
    ** To whom correspondence should be addressed. E-mail: marco@nmr.kun.nl

